Zayed University ZU Scholars

All Works

10-1-2021

# Sustainable maritime crude oil transportation: a split pickup and split delivery problem with time windows

Hiba Yahyaoui Zayed University

Nadia Dahmani Zayed University, nadia.dahmani@zu.ac.ae

Saoussen Krichen Institut Supérieur de Gestion de Tunis

Follow this and additional works at: https://zuscholars.zu.ac.ae/works

Part of the Computer Sciences Commons, and the Engineering Commons

## **Recommended Citation**

Yahyaoui, Hiba; Dahmani, Nadia; and Krichen, Saoussen, "Sustainable maritime crude oil transportation: a split pickup and split delivery problem with time windows" (2021). *All Works*. 4585. https://zuscholars.zu.ac.ae/works/4585

This Article is brought to you for free and open access by ZU Scholars. It has been accepted for inclusion in All Works by an authorized administrator of ZU Scholars. For more information, please contact scholars@zu.ac.ae.





Available online at www.sciencedirect.com



Procedia Computer Science 192 (2021) 4300-4309

Procedia Computer Science

www.elsevier.com/locate/procedia

## 25th International Conference on Knowledge-Based and Intelligent Information & Engineering Systems

## Sustainable maritime crude oil transportation: a split pickup and split delivery problem with time windows

Hiba Yahyaoui<sup>a,b,\*</sup>, Nadia Dahmani<sup>a,b</sup>, Saoussen Krichen<sup>b</sup>

<sup>a</sup>Zayed University, College of Technological Innovation, Abu Dhabi, UAE <sup>b</sup>Institut Supérieur de Gestion de Tunis, LARODEC, University of Tunis, Tunisia

#### Abstract

This paper studies a novel sustainable vessel routing problem modeling considering the multi-compartment, split pickup and split delivery, and time windows concepts. In the presented problem, oil tankers transport crude oil from supply ports to demand ports around the globe. The objective is to find ship routes, as well as port arrival and departure times, in a way that minimizes transportation costs. As a second objective, we considered the sustainability aspect by minimizing the vessel energy efficiency operational indicator. Multiple products are transported by a heterogeneous fleet of tankers. Small realistic test instances are solved with the exact method.

© 2021 The Authors. Published by Elsevier B.V. This is an open access article under the CC BY-NC-ND license (https://creativecommons.org/licenses/by-nc-nd/4.0) Peer-review under responsibility of the scientific committee of KES International.

Keywords: Sustainable transportation, Maritime crude oil, pickup and delivery, multi-objective problem, EEOI

#### 1. Introduction

According to the International Energy Agency [28], over the past century, the growth in the global economy has an impact on the environment, that led to increased use of energy and emissions of greenhouse gases (GHG).

The International Transport Forum [29] estimated that maritime transport is responsible of 873 million tonnes of CO2 per year [29], according to [27] ships accounted for approximately 1 billion tonnes of GHG emissions over the period 2007 to 2012. Besides, oil tankers make approximately 114 million tonnes of CO2 [26], about 13% of maritime emissions.

In this paper, a Multi-Compartment Vehicle Routing Problem (MCVRP) in maritime transportation is addressed. In ship routing problems, the multiple compartments concept is commonly used due to its importance in the transportation of different products via large ships. In fact, ships pick up the products to be transported from supply ports, then deliver them to demand ports based on a schedule. Besides, ships are loaded with different types of products, in sepa-

<sup>\*</sup> Corresponding author. Tel.:

E-mail address: hiba.yahyawi@gmail.com

<sup>1877-0509 © 2021</sup> The Authors. Published by Elsevier B.V.

This is an open access article under the CC BY-NC-ND license (https://creativecommons.org/licenses/by-nc-nd/4.0) Peer-review under responsibility of the scientific committee of KES International.

<sup>10.1016/</sup>j.procs.2021.09.206

rate compartments with fixed sizes [25], then these compartments are shared between customers.

In recent literature, most to ship routing problems studies considered multi-compartments with flexible products assignment. In the crude oil transportation domain, refineries order crude oil to produce a panoply of petroleum products [10]. For this reason, they require different quality of crude oil, thus, the transportation planning needs to be treated as multi-compartment. Furthermore, several papers have studied the problem of minimizing the CO2 and GHG emission as key sustainability aspect to avoid the most catastrophic impacts of climate change.

In [15], the authors proposed a mixed integer non-linear programming model that includes the issues pertaining to multiple time horizons, sustainability aspects and varying demand and supply at various ports. They proposed an effective particle swarm optimization-composite particle metaheuristic to solve the problem. In their paper, they integrated the carbon emission, fuel cost and fuel consumption constraints to the mathematical model for encapsulating the sustainability dimensions.

The sustainability in maritime transportation problem was presented in [17], the authors studied a multi-objective ship routing and scheduling problem that includes time window concept. To tackle the problem, they developed a sorting genetic algorithm II (NSGA-II) and particle swarm optimization metaheuristics. [19] addressed the sustainable ship routing problem considering a time window concept and bunker fuel management. The objective is reducing carbon emissions within the maritime transportation domain. The problem is solved with a hybrid particle swarm optimization and a basic variable neighborhood search algorithm.

The maritime transportation sector is a significant emitter of carbon dioxide, the amount of which is directly proportional to fuel consumption. The International Maritime Organization (IMO) introduced the Energy Efficiency Operation Index (EEOI) in 2009 [4] and encouraged the voluntary use of this metric in order to facilitate the evaluation of CO2 emission and fuel efficiency. Consequently, EEOI is further highlighted in 2016 [30]. The EEOI is originally formulated for policy purposes by the European Commission's proposal between EU ports [14]. The basic formulation of the EEOI for a ship journey is defined as the mass of CO2 per unit of transport work, i.e. grams of CO2 emission per barrel-nautical miles [18].

#### 2. Problem description

Global shipping companies plan vessels' routes and schedules in a particular planning horizon to reduce the overall transportation cost, see figure 1. On the other hand they take into account the sustainability aspects. In this context, our model considers two objectives which are the minimization of the voyage costs  $Total_{cost}$  that covers the travel costs (in the sea)  $C^{Sea}$  and port costs  $C^{Port}$  and the minimization of the EEOI.

$$min \ Total_{cost} = C^{Sea} + C^{Port} \tag{1}$$

### Travel costs C<sup>Sea</sup>

- Sailing cost  $C_1$ . Incurs the sailing cost for vessel v on an entire route.
- Sea fuel cost (traveling)  $C_2$ . Depicts the fuel consumption cost for vessel while sailing in sea
- Sea fuel cost (waiting)  $C_3$ . Accounts the fuel consumption for the waiting time (idle).

#### where:

- $C^{v}$ : route cost for vessel v
- $F_v^{sea}$  fuel consumption rate while sailing per unit time for vessel v
- $T_{ij}$ : travel time between ports *i* and port *j*
- $F_v^{wait}$ : fuel consumption rate while waiting per unit time for vessel v
- *wt*<sub>*iv*</sub>: vessel *v* waiting time at port *i*

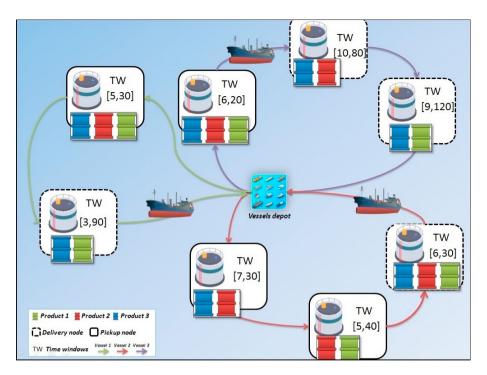


Fig. 1. Maritime crude oil transportation

$$C^{Sea} = \underbrace{\sum_{v \in V} \sum_{i \in N} \sum_{j \in N} C^v x_{ijv}}_{V \in V} + \underbrace{\sum_{v \in V} \sum_{i \in N} \sum_{j \in N} F_v^{sea} t_{ij} x_{ijv}}_{V \in V} + \underbrace{\sum_{v \in V} \sum_{i \in N} F_v^{wait} w t_{iv}}_{V \in V}$$
(2)

## Port costs C<sup>Port</sup>

- Handling cost C<sub>4</sub>. Covers the variable part of the costs in a port. The fuel consumption in a port depends on the amount of handled cargo.
- Port operating cost  $C_5$ . Depicts the fixed cost for performing port's loading/unloading operation.
- Docking cost  $C_6$ . Provides a port's docking charges.

#### where:

- $C_i^q$ : cost per weight unit for pickup or delivery in port *i*
- $q_{ip}$ : requirement: cargo weight to be picked up/delivered of product p in port i
- $y_{iv}$ : Binary variable; = 1, if vessel v visit port i and 0 otherwise
- $R_{iv}$ : fixed cost for performing loading/unloading operation of vessel v at port i
- *O*<sub>*iv*</sub>: docking cost of a vessel *v*
- *st<sub>i</sub>*: vessel service time at port *i*

$$C^{Port} = \overbrace{\sum_{v \in V} \sum_{i \in N} C_i^q q_{ip} y_{iv}}^{C4} + \overbrace{\sum_{i \in N} \sum_{v \in V} R_{iv} y_{iv}}^{C5} + \overbrace{\sum_{i \in N} \sum_{v \in V} O_{iv} y_{iv} st_i}^{C6}$$
(3)

The Energy Efficiency Operation Indicator (EEOI), one of schemes as a monitoring performance indicator related to the vessel energy efficiency management plan which is the mandatory regulation for vessels in operation, intending to reduce greenhouse gas emissions in maritime transportation. It is closely related to vessel speed and the waterway environment, among other factors. Finding the optimal main engine speed is a basic way to improve energy efficiency and reduce the EEOI [21]. The EEOI, an important indicator of vessel energy efficiency stipulated by the international maritime organization, was firstly introduced in 2011 [4] as follows, where:

- $F_{ijv}$ : the fuel consumption for vessel v on arc (i, j)
- $C_F$ : conversion factor between fuel consumption and CO2 emission
- *Dist<sub>ij</sub>*: distance between port *i* and *j*
- *S*<sub>s</sub>: average sailing speed

$$\min \quad \frac{\sum_{v \in V} \sum_{i \in N} \sum_{j \in N} F_{ijv}.C_F}{\sum_{v \in V} \sum_{i \in N} \sum_{j \in N} S_s Dist_{ij}} \mathbf{x}_{ijv} \tag{4}$$

**Fuel consumption.** According to [18], fuel consumption  $F_{ijv}$ , can be expressed as follows, where:

- $S_v$ : design speed for vessel v
- $\nabla_{ijv}$ : vessel v's displacement on arc (i, j)
- $\nabla_v$ : the full load displacement for vessel *v*
- $F_{dv}$ : the design daily fuel consumption at design speed for vessel v
- $T_{ij}$ : travel time between ports *i* and port *j*

$$F_{ij\nu} = (\frac{S_s}{S_{\nu}})^n . (\frac{\nabla_{ij\nu}}{\nabla_{di}})^{2/3} . F_{d\nu} . T_{ij}$$
(5)

Concerning the constraints, we consider the multi-compartment constraints, split pickup and split delivery constraints, time windows constraints, and the vessel routing constraints as given in [10].

Multi-compartment, pickup and delivery constraints. impose both the capacity and connectivity of the feasible arcs [20] [9].

**Cargo restrictions and vessel load balance constraints.** restrict cargo weight and volume on arcs. The total cargo amount onboard a vessel has to be less than or equal to a weight or volume limit. Each arc has a cargo weight, cargo volume or both, cargo weight and volume, restriction.

**Vessel routing constraints.** ensure that each port is visited by exactly one vessel, and the continuity of each route, that is: a vessel that visits a port must leave it, it guarantees the continuity of vessel' pathways. Then, it states that if there is a vessel travel from port 1 to port 2, they are visited by the same vessel.

**Time windows constraints.** represent a soft time windows constraints. It guarantees that the serves to a port must be within a given time windows. Also, it ensures that the starting time of the next port has to consider the start serve time plus the waiting time and the service time of the previous port, in addition to the travel time between the two ports.

#### 3. Experimental study

We present in this section the results of randomly generated instances using Ilog CPLEX. The instances parameters' values were tuned based on the ranges reported in table 3. In table 1, we report more details about the artificial instances;

- the number of ports are between 5 and 20
- vessels are between 3 and 9

- two categories of product numbers |P|: 2 and 3
- Two ranges of the Pickup & delivery: [30%, 70%] and [50%, 50%]
- three types of time windows: Without Time windows (WTW), Narrow Time windows (NTW), and Time windows (TW)

Our experiments were executed on a personal computer with *Intel Core<sup>TM</sup>* i7-4610M CPU @ 3.00GHz 3.00GHz 16 GB RAM and Windows 8.1 pro, 64-bit operating system, x64-based processor.

We considered a vessel named MARPOL tanker of IMO's oil tanker classification, shown in figure 2. The ship characteristics are given in table 2.

Table 4 reports the generated solution values. *Inst.* refers to the instance name, n, v are respectively the number of ports and vessels, p is the number of the considered products, P/D are the number of pickup and delivery ports respectively, and TW is the time windows type for that instance.

In this table we recorded the total cost, *opt.*, means that the obtained result is an optimal solution, the different costs, and the EEOI value for that solution.

We plotted in figure 3 the graphical representation of the results showing the impact of the time windows types on the total cost. We can notice from this figure that the narrow time windows (NTW) requires the highest cost comparing to the other two types of time windows.

In figure 4, we pointed out the impact of the time windows types on EEOI. We can see that in the NTW instances the EEOI is higher than the WTW instances and TW instances. Hence, we can conclude that if the time windows is more tight, the it has a negative impact on the environment, as the vessel needs to use the maximum allowed speed.

There are many different methods for multi-objective optimization, as a common concept, minimizing a weighted sum constitutes an independent method as well as a component of other methods. In this study we used the weights as the equation bellow.

$$Min \ w_1 * obj_1 + w_2 * obj_2 \quad where \quad w_1 + w_2 = 1$$
(6)

The bi-objective model was assessed using multi-objective metrics. These metrics are detailed in what follows. Table 5 reports the multi-objective performance metrics.

- Cardinality of the Pareto set (Card): This metric is to measure the cardinality of the potentially efficient set, it counts the total number of non-dominated solutions.
- Diversification metric (Div): The diversification metric (Div) is to indicate the diversity of the Pareto solutions. The Div is calculated using the following equation.

$$Div = \sqrt{\sum_{i=1}^{N_{abj}} (\max_{j=1..card} \{obj_i^j\} \min_{j=1..card} \{obj_i^j\})^2}$$
(7)

• Spacing (Sp): The spacing metric is to determine the distribution of solutions in an obtained Pareto Front.

$$Sp = \sqrt{\frac{1}{Card - 1} \sum_{i=1}^{Card} (t - d_i)^2}$$
(8)

Ports, Vessels	P	Pickup & delivery	Time windows
5,3	2	30% , 70%	Without Time windows (WTW)
10,4	3	··· , ···	Narrow Time windows (NTW)
15,7		50% , 50%	Time windows (TW)
20,9			

Table 1. Artificial instances



Fig. 2. The oil tanker: MARPOL tanker of IMO's oil tanker classification

#### MODEL DIMENSIONS

Length overall	183cm
Breadth	30cm
Depth	15.8cm
Draught	10.6cm
Freeboard	5.2cm

Table 2. Ship characteristics

$$d_{i} = \min_{k} \sum_{m=1}^{N_{obj}} |ob j_{m}^{i} - ob j_{m}^{k}|, k = 1, .., Cardandi \neq k$$
(9)

• Time (Avg time): The average computing time reported by the tested methods

#### 4. Conclusions

In this paper we studied a new multi-objective version of the sustainable vessel routing problem. The first objective encompasses different costs related to vessel sailing and docking time at port. The second objective is the minimization of the greenhouse emissions expressed with the vessel energy efficiency operational indicator. The considered constraints are related to multi-compartment, split pickup and split delivery, and time windows concepts. The pro-

Parameter or variable		Range	Unit
Cost per weight unit for operations	$C_i^q$	[2,8]	USD/Gallon
Requirement: cargo weight	$q_{ip}$	[500,1000]	Gallon
Route cost for sailing	$C_{ii}^{v}$	[30,80]	USD
The docking cost	$O_{iv}$	[100,500]	USD/hours
Maximum allowed cargo weight	$W_{ijv}$	[2000,4000]	Gallons
Maximum allowed cargo volume	$V_{ijv}$	[16.7,33.38]	Kg/Gallon
Density of product	$D_p$	119.826	Kg/Gallon
Travel time between ports	$t_{ij}$	[12.18]	hours
Distance between ports	$Dis_{ij}$	[300.500]	Nautical Miles (nm)
Fuel consumption rate while sailing	$F_v^{sea}$	[30,80]	USD/nm
Fuel consumption rate while waiting	$F_v^{wait}$	[10,50]	USD/hours
Design speed for vessel	$S_{v}$	30	knots
Vessel type specific power parameter	8	3	-
Design daily fuel consumption	$F_{v}$		
Sufficiently large number	М	1000	-
Average sailing speed	$S_{ijv}$	{12,16,22}	knots

Table 3. Artificial instances ranges

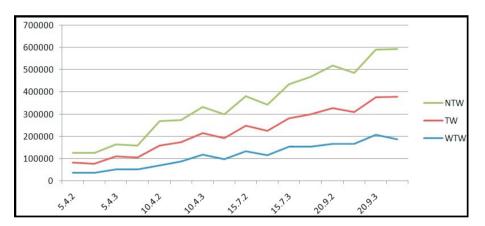


Fig. 3. Graphical representation of the results: the impact of the time windows on the total cost

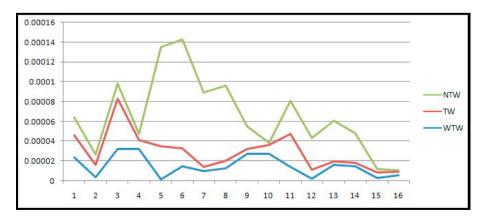


Fig. 4. Graphical representation of the results: the impact of the time windows on the EEOI

	n, v	р	P/D	<i>T.W</i> .	CPL					Costs (USE	,	-		EEOI
					Total <sub>Cost</sub>	Туре			costs			Port cost:		
							$C_1$	$C_2$	$C_3$	#	$C_4$	$C_5$	#	
$C_{01}$	5,4	2	2/3	WTW	35618	Opt.	303	12408	1548	14259	20058	1302	21360	24.6×10 <sup>-5</sup>
$C_{02}$	- /		7-	NTW	43124	Opt.	296	15530	126	15952	26095	1077	27172	18.57×10 <sup>-5</sup>
$C_{03}$				TW	46156	Opt.	301	15733	190	29233	28927	1006	16224	$22.52 \times 10^{-5}$
$C_{04}$			3/2	WTW	35840	Opt.	339	20060	390	20789	13710	1341	15051	39.2×10 <sup>-6</sup>
$C_{05}$				NTW	48434	Opt.	325	19975	2409	22709	24329	1396	25725	11.88×10 <sup>-5</sup>
$C_{06}$				TW	39.898	Opt.	302	13590	0	13892	24840	1167	26007	12.31×10 <sup>-5</sup>
$C_{07}$		3	2/3	WTW	52046	Opt.	322	14235	2175	16732	33867	1447	35314	32×10 <sup>-5</sup>
$C_{08}$		5	2,5	NTW	55428	Opt.	320	20874	378	21572	32690	1167	33857	$15.9 \times 10^{-5}$
$C_{09}$				TW	56259	Opt.	298	14450	929	15677	38998	1585	40583	51.44×10 <sup>-5</sup>
						-								
$C_{10}$			3/2	WTW	50531	Opt.	285	18450	580	19315	29712	1504	31216	32.8×10 <sup>-5</sup>
$C_{11}$				NTW	55663	Opt.	350	21394	0	21744	32467	1452	33919	$61.05 \times 10^{-6}$
$C_{12}$				TW	52578	Opt.	300	24043	770	25113	26436	1029	27465	93.4×10 <sup>-6</sup>
C <sub>13</sub>	10,4	2	3/7	WTW	68697	Opt.	571	19770	_	20341	45801	2555	48356	17.8×10 <sup>-6</sup>
$C_{14}^{13}$				NTW	111596	Opt.	977	62263	0	63240	45801	2555	48356	0.001
$C_{15}$			1	TW	87878	Opt.	776	37442	1304	39522	45001	2555	48356	33.226×10-
~					0.000.	0	0.7.0	202-7-	0	418-55	10		15005	
$C_{16}$			5/5	WTW	86804	Opt.	830	38267	2672	41769	42510	2525	45035	$15 \times 10^{-5}$
$C_{17}$				NTW TW	99180 87092	Opt. Opt.	917 765	48016 36119	39 0	48972 36884	47587 47587	2621 2621	50208 50208	0.0011 17.77×10 <sup>-6</sup>
$C_{18}$				1 W	87092	Opi.	703	50119	0	30884	47387	2021	30208	17.77×10
$C_{19}$		3	3/7	WTW	118122	Opt.	805	45636	1484	47925	66713	3484	70197	10.7×10 <sup>-5</sup>
$C_{19}$ $C_{20}$		5	5/1	NTW	117640	Opt.	853	56594	102	57549	57106	2985	60091	$75.1 \times 10^{-5}$
$C_{20}$ $C_{21}$				TW	96082	Opt.	638	29240	2734	32612	60980	2490	63470	41.17×10 <sup>-6</sup>
- 21				1		• 1								
$C_{22}$			5/5	WTW	97641	Opt.	813	30299	1799	32911	62317	2413	64730	$13.8 \times 10^{-5}$
$C_{23}$				NTW	107008	Opt.	963	41192	124	42279	62317	2413	64730	76.06×10 <sup>-5</sup>
$C_{24}$				TW	92820	Opt.	746	26994	250	28090	62317	2413	64730	71.78×10 <sup>-6</sup>
$C_{25}$	15,7	2	5/10	WTW	131874	Opt.	1308	79464	1330	82102	45398	4374	49772	27.9×10 <sup>-5</sup>
$C_{26}$	- ) -		- / -	NTW	133428	Opt.	1346	80757	1553	83656	45398	4374	49772	23.711×10-
$C_{27}^{20}$				TW	115764	Opt.	1148	58914	65	60127	51562	4075	55637	49.15×10 <sup>-6</sup>
				'										
									-	-	_	_	_	_
			7/8	WTW	-	Opt.	-	-						
$C_{28} \\ C_{29}$			7/8	NTW	117064	Opt.	1053	60633	189	61875	51356	3833	55189	23.6×10 <sup>-6</sup>
$C_{29}$			7/8											23.6 ×10 <sup>-6</sup> 93.78×10 <sup>-6</sup>
C <sub>29</sub> C <sub>30</sub>		3		NTW TW	117064 111609	Opt. Opt.	1053 1007	60633 54447	189 1080	61875 56534	51356 51046	3833 4030	55189 55076	93.78×10 <sup>-6</sup>
$C_{29}$ $C_{30}$ $C_{31}$		3	7/8 5/10	NTW TW	117064 111609 151938	Opt. Opt. Opt.	1053 1007 1381	60633 54447 70320	189 1080 1170	61875 56534 72871	51356 51046 74993	3833 4030 4075	55189 55076 79068	93.78×10 <sup>-6</sup> 14.5 ×10 <sup>-5</sup>
$C_{29} \\ C_{30} \\ C_{31} \\ C_{32}$		3		NTW TW	117064 111609 151938 155612	Opt. Opt. Opt. Opt.	1053 1007 1381 1443	60633 54447 70320 74872	189 1080	61875 56534 72871 76544	51356 51046 74993 74993	3833 4030 4075 4075	55189 55076 79068 79068	93.78×10 <sup>-6</sup> 14.5×10 <sup>-5</sup> 34.3×10 <sup>-5</sup>
$C_{29} \\ C_{30} \\ C_{31} \\ C_{32}$		3		NTW TW	117064 111609 151938	Opt. Opt. Opt.	1053 1007 1381	60633 54447 70320	189 1080 1170 229	61875 56534 72871	51356 51046 74993	3833 4030 4075	55189 55076 79068	93.78×10 <sup>-6</sup> 14.5×10 <sup>-5</sup>
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$		3		NTW TW	117064 111609 151938 155612	Opt. Opt. Opt. Opt.	1053 1007 1381 1443	60633 54447 70320 74872	189 1080 1170 229	61875 56534 72871 76544	51356 51046 74993 74993	3833 4030 4075 4075	55189 55076 79068 79068	93.78×10 <sup>-6</sup> 14.5×10 <sup>-5</sup> 34.3×10 <sup>-5</sup> 33.8×10 <sup>-6</sup>
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$		3	5/10	NTW TW WTW NTW TW	117064 111609 151938 155612 128217 152242 167507	Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007	60633 54447 70320 74872 57862	189 1080 1170 229 625	61875 56534 72871 76544 59494	51356 51046 74993 74993 64408	3833 4030 4075 4075 4315	55189 55076 79068 79068 68723	$93.78 \times 10^{-6}$ $14.5 \times 10^{-5}$ $34.3 \times 10^{-5}$ $33.8 \times 10^{-6}$ $25.87 \times 10^{-6}$ $33.07 \times 10^{-5}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$		3	5/10	NTW TW WTW NTW TW	117064 111609 151938 155612 128217 152242	Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325	60633 54447 70320 74872 57862 80356	189 1080 1170 229 625 1260	61875 56534 72871 76544 59494 82941	51356 51046 74993 74993 64408 65125	3833 4030 4075 4075 4315 4176	55189 55076 79068 79068 68723 69301	$93.78 \times 10^{-6}$ $14.5 \times 10^{-5}$ $34.3 \times 10^{-5}$ $33.8 \times 10^{-6}$ $25.87 \times 10^{-6}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$		3	5/10	NTW TW NTW TW WTW NTW	117064 111609 151938 155612 128217 152242 167507	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417	60633 54447 70320 74872 57862 80356 85507	189 1080 1170 229 625 1260 229	61875 56534 72871 76544 59494 82941 87153	51356 51046 74993 74993 64408 65125 76401	3833 4030 4075 4075 4315 4176 3954	55189 55076 79068 79068 68723 69301 80355	$93.78 \times 10^{-6}$ $14.5 \times 10^{-5}$ $34.3 \times 10^{-5}$ $33.8 \times 10^{-6}$ $25.87 \times 10^{-6}$ $33.07 \times 10^{-5}$
$\begin{array}{c} C_{29} \\ C_{30} \\ \end{array}$ $\begin{array}{c} C_{31} \\ C_{32} \\ C_{33} \\ \end{array}$ $\begin{array}{c} C_{34} \\ C_{35} \\ \end{array}$ $\begin{array}{c} C_{36} \\ \end{array}$	20,9		5/10	NTW TW       WTW NTW TW       WTW WTW       WTW       WTW	117064 111609 151938 155612 128217 152242 167507 146995 165320	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766	60633 54447 70320 74872 57862 80356 85507 64248 83956	189 1080 1170 229 625 1260 229 65 3764	61875 56534 72871 76544 59494 82941 87153 65383 89486	51356 51046 74993 74993 64408 65125 76401 77231 70305	3833 4030 4075 4075 4315 4176 3954 4381 5529	55189 55076 79068 79068 68723 69301 80355 81612 75834	$93.78 \times 10^{-6}$ $14.5 \times 10^{-5}$ $34.3 \times 10^{-5}$ $33.8 \times 10^{-6}$ $25.87 \times 10^{-6}$ $33.07 \times 10^{-5}$ $82.72 \times 10^{-6}$ $16.24 \times 10^{-5}$
$\begin{array}{c} C_{29} \\ C_{30} \\ \end{array}$ $\begin{array}{c} C_{31} \\ C_{32} \\ C_{33} \\ \end{array}$ $\begin{array}{c} C_{34} \\ C_{35} \\ \end{array}$ $\begin{array}{c} C_{36} \\ \end{array}$ $\begin{array}{c} C_{37} \end{array}$	20,9		5/10 7/8	NTW TW       WTW NTW TW       WTW NTW       WTW NTW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060	189 1080 1170 229 625 1260 229 65	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737	55189 55076 79068 79068 68723 69301 80355 81612 75834 73733	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ 16.24 \times 10^{-5} \\ 41.03 \times 10^{-5} \end{array}$
$\begin{array}{c} C_{29} \\ C_{30} \\ \\ C_{31} \\ C_{32} \\ C_{33} \\ \\ C_{34} \\ C_{35} \\ C_{36} \\ \\ \\ \end{array}$	20,9		5/10 7/8	NTW TW       WTW NTW TW       WTW WTW       WTW       WTW	117064 111609 151938 155612 128217 152242 167507 146995 165320	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766	60633 54447 70320 74872 57862 80356 85507 64248 83956	189 1080 1170 229 625 1260 229 65 3764	61875 56534 72871 76544 59494 82941 87153 65383 89486	51356 51046 74993 74993 64408 65125 76401 77231 70305	3833 4030 4075 4075 4315 4176 3954 4381 5529	55189 55076 79068 79068 68723 69301 80355 81612 75834	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ \end{array}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$ $C_{37}$ $C_{38}$ $C_{39}$	20,9		5/10 7/8 6/14	NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740	189 1080 1170 229 625 1260 229 65 3764 354 369	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946	55189 55076 79068 79068 68723 69301 80355 81612 75834 73733 77593	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ 16.24 \times 10^{-5} \\ 41.03 \times 10^{-5} \\ 34.16 \times 10^{-6} \end{array}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$ $C_{37}$ $C_{38}$ $C_{39}$ $C_{40}$	20,9		5/10 7/8	NTW TW       WTW NTW TW       WTW NTW TW       WTW       WTW       WTW       WTW       WTW       WTW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259 164200	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557 1781	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740 83256	189 1080 1170 229 625 1260 229 65 3764 354 369 4926	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666 89963	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647 68683	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946 5555	55189 55076 79068 79068 68723 69301 80355 81612 75834 73733 77593 74238	$93.78 \times 10^{-6}$ $14.5 \times 10^{-5}$ $34.3 \times 10^{-5}$ $33.8 \times 10^{-6}$ $25.87 \times 10^{-6}$ $33.07 \times 10^{-5}$ $82.72 \times 10^{-6}$ $16.24 \times 10^{-5}$ $41.03 \times 10^{-5}$ $34.16 \times 10^{-6}$ $15.6 \times 10^{-5}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$ $C_{37}$ $C_{38}$ $C_{39}$ $C_{40}$ $C_{41}$	20,9		5/10 7/8 6/14	NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740	189 1080 1170 229 625 1260 229 65 3764 354 369	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946	55189 55076 79068 79068 68723 69301 80355 81612 75834 73733 77593	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ 16.24 \times 10^{-5} \\ 41.03 \times 10^{-5} \\ 34.16 \times 10^{-6} \end{array}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$ $C_{37}$ $C_{38}$ $C_{39}$ $C_{40}$ $C_{41}$	20,9		5/10 7/8 6/14	NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW       WTW NTW       WTW NTW       WTW NTW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259 164200 177552	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557 1781 1988	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740 83256 103750	189 1080 1170 229 625 1260 229 65 3764 354 369 4926 159	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666 89963 10590	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647 68683 66039	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946 5555 5618	55189 55076 79068 79068 68723 69301 80355 81612 75834 73733 77593 74238 71657	$93.78 \times 10^{-6}$ $14.5 \times 10^{-5}$ $34.3 \times 10^{-5}$ $33.8 \times 10^{-6}$ $25.87 \times 10^{-6}$ $33.07 \times 10^{-5}$ $82.72 \times 10^{-6}$ $16.24 \times 10^{-5}$ $41.03 \times 10^{-5}$ $15.6 \times 10^{-5}$ $30.7 \times 10^{-5}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$	20,9		5/10 7/8 6/14	NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW       WTW WTW       WTW       WTW       WTW       WTW       WTW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259 164200 177552 143922	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557 1781 1988 1619 -	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740 83256 103750 71710 -	189 1080 1170 229 625 1260 229 65 3764 354 369 4926 159 .875 -	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666 89963 10590 74204	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647 68683 66039 64335	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946 5555 5618 .5384 -	55189 55076 79068 68723 69301 80355 81612 75834 73733 77593 74238 71657 69719 -	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ 15.6 \times 10^{-5} \\ 34.16 \times 10^{-5} \\ 30.7 \times 10^{-5} \\ 29.96 \times 10^{-6} \\ -\end{array}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$ $C_{37}$ $C_{38}$ $C_{39}$ $C_{40}$ $C_{41}$ $C_{42}$ $C_{42}$ $C_{43}$ $C_{44}$	20,9	2	5/10 7/8 6/14 10/10	NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259 164200 177552 143922	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557 1781 1988 1619 	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740 83256 103750 71710 -	189 1080 1170 229 625 1260 229 65 3764 354 369 4926 159 .875 - 354	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666 89963 10590 74204 - 113370	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647 68683 66039 64335	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946 5555 5618 .5384 - 5270	55189 55076 79068 79068 68723 69301 80355 81612 75834 73733 77593 74238 71657 69719 – 102530	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ 15.6 \times 10^{-5} \\ 34.16 \times 10^{-5} \\ 29.96 \times 10^{-6} \\ - \\ 42.72 \times 10^{-6} \end{array}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$ $C_{37}$ $C_{38}$ $C_{39}$ $C_{40}$ $C_{41}$ $C_{42}$	20,9	2	5/10 7/8 6/14 10/10	NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW       WTW WTW       WTW       WTW       WTW       WTW       WTW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259 164200 177552 143922	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557 1781 1988 1619 -	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740 83256 103750 71710 -	189 1080 1170 229 625 1260 229 65 3764 354 369 4926 159 .875 -	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666 89963 10590 74204	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647 68683 66039 64335	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946 5555 5618 .5384 -	55189 55076 79068 68723 69301 80355 81612 75834 73733 77593 74238 71657 69719 -	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ 15.6 \times 10^{-5} \\ 34.16 \times 10^{-5} \\ 30.7 \times 10^{-5} \\ 29.96 \times 10^{-6} \\ -\end{array}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$ $C_{37}$ $C_{38}$ $C_{39}$ $C_{40}$ $C_{41}$ $C_{42}$ $C_{42}$ $C_{43}$ $C_{44}$ $C_{45}$	20,9	2	5/10 7/8 6/14 10/10 6/14	NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259 164200 177552 143922 - 215900 169581	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557 1781 1988 1619 - 1997 1579	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740 83256 103750 71710 - 111020 76779	189 1080 1170 229 625 1260 229 65 3764 354 369 4926 159 .875 - 354 785	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666 89963 10590 74204 - 113370 79143	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647 68683 66039 64335 - 97257 85119	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946 5555 5618 .5384 - 5270 5319	55189 55076 79068 79068 68723 69301 80355 81612 75834 73733 77593 74238 71657 69719 - 102530 90438	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ 16.24 \times 10^{-5} \\ 34.16 \times 10^{-6} \\ 15.6 \times 10^{-5} \\ 29.96 \times 10^{-6} \\ - \\ 42.72 \times 10^{-6} \\ 51.76 \times 10^{-6} \end{array}$
$C_{29}$ $C_{30}$ $C_{31}$ $C_{32}$ $C_{33}$ $C_{33}$ $C_{34}$ $C_{35}$ $C_{36}$ $C_{37}$ $C_{38}$ $C_{39}$ $C_{40}$ $C_{41}$ $C_{42}$ $C_{42}$ $C_{43}$ $C_{44}$	20,9	2	5/10 7/8 6/14 10/10	NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW       WTW NTW TW	117064 111609 151938 155612 128217 152242 167507 146995 165320 192174 162259 164200 177552 143922	Opt. Opt. Opt. Opt. Opt. Opt. Opt. Opt.	1053 1007 1381 1443 1007 1325 1417 1070 1766 2023 1557 1781 1988 1619 	60633 54447 70320 74872 57862 80356 85507 64248 83956 116060 82740 83256 103750 71710 -	189 1080 1170 229 625 1260 229 65 3764 354 369 4926 159 .875 - 354	61875 56534 72871 76544 59494 82941 87153 65383 89486 118440 84666 89963 10590 74204 - 113370	51356 51046 74993 74993 64408 65125 76401 77231 70305 67996 71647 68683 66039 64335	3833 4030 4075 4075 4315 4176 3954 4381 5529 5737 5946 5555 5618 .5384 - 5270	55189 55076 79068 79068 68723 69301 80355 81612 75834 73733 77593 74238 71657 69719 – 102530	$\begin{array}{c} 93.78 \times 10^{-6} \\ 14.5 \times 10^{-5} \\ 34.3 \times 10^{-5} \\ 33.8 \times 10^{-6} \\ 25.87 \times 10^{-6} \\ 33.07 \times 10^{-5} \\ 82.72 \times 10^{-6} \\ 15.6 \times 10^{-5} \\ 34.16 \times 10^{-5} \\ 29.96 \times 10^{-6} \\ - \\ 42.72 \times 10^{-6} \end{array}$

Ports	Vessels	P	Card	Div	S P	Time (s)
5	3	2	3	5	1.68069	1.82
5	3	3	4	6	1.71069	1.92
10	4	2	5	8	1.8895	4.9
10	4	3	5	10	1.98910	4.11
15	7	2	6	11	1.08069	5.81
15	7	3	8	13	1.5238	6.56
20	9	2	9	12	1.6069	9.73
20	9	3	11	12	1.8654	11.43

Table 5. Multi-objective performance metrics

posed model is tested on CPLEX using random generated instances based on a real case study. The computational results show that the narrow time windows requires the highest cost and greenhouse emissions.

#### References

- E. T. Iakovou. An interactive multiobjective model for the strategic maritime transportation of petroleum products: risk analysis and routing. Safety Science 39, 19–29, 2001
- [2] Marine Environment Protection Committee, 2011. Report of the Marine Environment Protection Committee on its Sixty-Second Session. IMO, London, p. 7.
- [3] F. Hennig, B. Nygreen, K. C. Furman, J. Song and G. R. Kocis. Crude Oil Tanker Routing and Scheduling. INFOR, Vol. 49, No. 2, pp. 153–170, 2011
- [4] Marine Environment Protection Committee, 2011. Report of the Marine Environment Protection Committee on its Sixty-Second Session. IMO, London, p. 7.
- [5] F. Hennig, B. Nygreen, M. Christiansen, K. Fagerholt, K.C. Furman, J. Song, G.R. Kocis, and P.H. Warrick. Maritime crude oil transportation – A split pickup and split delivery problem. European Journal of Operational Research 218(3):764-774, 2012
- [6] F. Hennig, B. Nygreen and M. E. Lubbecke. Nested column generation applied to the crude oil tanker routing and scheduling problem with split pickup and split delivery. Naval Research Logistics 59 (3-4) 298-310 2012
- [7] L. Aizemberg, H. H. Kramer, A. A. Pessoa, E. Uchoa. Formulations for a problem of petroleum transportation. European Journal of Operational Research 237(1): 82-90, 2014
- [8] T. Nishi, T. Izuno. Column generation heuristics for ship routing and scheduling problems in crude oil transportation with split deliveriesn. Computers and Chemical Engineering 60(1): 329-338, 2014
- [9] M.M.S. Abdulkader, Y. Gajpal, T. ElMekkawy. Hybridized ant colony algorithm for the Multi Compartment Vehicle Routing Problem. Applied Soft Computing (37), 196-203, 2015
- [10] F. Hennig, B. Nygreen, K. C. Furman, and J. Song. Warrick. Alternative approaches to the crude oil tanker routing and scheduling problem with split pickup and split delivery. European Journal of Operational Research 243(1): 41-51, 2015
- [11] A. W. Siddiqui, M. Verma. A bi-objective approach to routing and scheduling maritime transportation of crude oil. Transportation Research Part D 37: 65-78, 2015
- [12] J. Lee, B. Kim. Industrial ship routing problem with split delivery and two types of vessels. Expert Systems With Applications 42 (22) 9012-9023. 2015
- [13] Y. Jiang and I. E.Grossmann. Alternative mixed-integer linear programming models of a maritime inventory routing problem. Computers and Chemical Engineering (77) 147-161. 2015
- [14] Parker, S. Raucci, C. Smith, T. Laffineur 2015. Understanding the Energy Efficiency Operational Indicator: and Empirical Analysis of Ships from the Belgian Shipowners' Association. Low Carbon Shipping report May 2015.jhttp://www.lowcarbonshipping.co.uk/files/Ben\_Howett/RBSA\_final\_main.pdf<sub>¿</sub>.

- [15] A. De, V. K. R. Mamanduru, A. Gunasekaran, N. Subramanian, and M. K. Tiwari. Composite particle algorithm for sustainable integrated dynamic ship routing and scheduling optimization. Computers and Industrial Engineering 96: 201-215, 2016
- [16] A. Veneti, A. Makrygiorgos, C. Konstantopoulos, G. Pantziou, and I. Vetsikas . Minimizing the fuel consumption and the risk in maritime transportation: a bi-objective weather routing approach. Computers and Operations Research 88: 220-236, 2017
- [17] A. De, A. Choudhary, and M. K. Tiwari. Multiobjective Approach for Sustainable Ship Routing and Scheduling With Draft Restrictions. IEEE Transactions on Engineering Managment 66 (1): 35-51, 2017
- [18] H. Jia. Crude oil trade and green shipping choices. Transportation Research Part D: Transport and Environment (65) 618-634. 2018
- [19] A. De, J. Wang, and M. K. Tiwari. Hybridizing Basic Variable Neighborhood Search With Particle Swarm Optimization for Solving Sustainable Ship Routing and Bunker Management Problem. IEEE Transactions on Intelligent Transportation Systems 21 (3): 986 - 997, 2019
- [20] I. Kaabachi, H. Yahyaoui, S. Krichen, A. Dekdouk. Measuring and evaluating hybrid metaheuristics for solving the multi-compartment vehicle routing problem. Measurement 141: 407-419, 2019
- [21] Y. H. Hou, K. Kang, X. Liang. Vessel speed optimization for minimum EEOI in ice zone considering uncertainty. Ocean Engineering (188), 106240, 2019
- [22] P. T. G. d. Santos, E. Kretschmannb, D. Borensteina, and P. C. Guedes. Cargo routing and scheduling problem in deep-sea transportation: Case study from a fertilizer company. Computers and Operations Research 119, 104934, 2020
- [23] L. Eide, G. C. H. Ardal, N. Evsikova, L. M. Hvattum, S. Urrutia. Load-dependent speed optimization in maritime inventory routing. Computers and Operations Research 123: 105051, 2020
- [24] C. Bagoulla, P. Guillotreau. Maritime transport in the French economy and its impact on air pollution: An input-output analysis. Marine Policy 116: 103818 2020
- [25] M. Ostermeier, T. Henke, A. Hubner, G. Wascherb. Multi-compartment vehicle routing problems: State-of-the-art, modeling framework and future directions. European Journal of Operational Research 292: 799–817, 2021
- [26] Olmer, N., Comer, B., Roy, B., Mao, X. and Rutherford, D. Greenhouse Gas Emissions from Global Shipping, 2013-2015. (2017), https://theicct.org/publications/ GHG-emissions-global-shipping-2013-2015 (last date of access 22-06-2020).
- [27] Smith, T. W. P., Jalkanen, J. P., Anderson, B. A., Corbett, J. J., Faber, J., Hanayama, S., and Pandey, A. (2015). Third IMO Greenhouse Gas Study 2014. Retrieved from http://www.imo.org/en/OurWork/Environment/Pollution/Prevention/AirPollution/ Documents/Third%20Greenhouse%20Gas%20Study/GHG3%20Executive%20Summary%20and%20Report.pdf
- [28] IEA (International Energy Agency), 2016. Key World Energy Statistics. http://www.iea.org/publications/freepublications/publication/KeyWorld2016.pdf
- [29] ITF, (2019) International Transport Forum and Organisation for Economic Co-operation and Development. ITF Transport Outlook 2019. OCEDiLibrary https://www.oecd-ilibrary.org/transport/itf-transport-outlook-2019\_transp\_outlook-en-2019-en
- [30] MEPC (Marine Environment Protection Committee). 2016. Guidelines for the development of a Ship Energy Efficiency Management Plan (SEEMP) MEPC 70/18. aspx¿.