

1-1-2021

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Recommended Citation

Zidan, Mohammed; Abdel-Aty, Abdel-Haleem; Khalil, Ashraf; Abdel-Aty, Mahmoud; and Eleuch, Hichem, "A Novel Efficient Quantum Random Access Memory" (2021). *All Works*. 4607.
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Date of publication xxxx 00, 0000, date of current version xxxx 00, 0000.

Digital Object Identifier 10.1109/ACCESS.2017.DOI

A Novel Efficient Quantum Random Access Memory

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ABSTRACT Owing to the significant progress in manufacturing desktop quantum computers, the quest to achieve efficient quantum random access memory (QRAM) became inevitable. In this paper, we propose a novel efficient random access memory for quantum computers. The proposed QRAM has a fixed structure and can be used efficiently to store both known and unknown classical/quantum data. The storage capacity of the proposed QRAM is more efficient than that of the classical RAMs and can be used to store both classical and quantum information. Furthermore, the proposed model can access an arbitrary location in $O(1)$ compared with other state-of-the-art models.

INDEX TERMS Quantum Random Access Memory, Quantum Circuits, Quantum Algorithm, Quantum Computers.

I. INTRODUCTION

The unique properties of quantum mechanics, i.e. superposition and entanglement, have revolutionized the speed of quantum computing. Quantum teleportation is a novel technology that can be used for transferring unknown quantum states [1], [2]. Previous research has shown that quantum computers solve complex computing problems faster than classical computers [3]–[9]. Recently, it has been proved that quantum computers can solve novel types of problems that are impossible to solve using classical computers [10]. Thus, the quest to achieve efficient quantum random access memory became inevitable. Also, the power of computing devices is based on the capacity to store information in an array of memory cells. Random access memory (RAM) is classified as an architecture for a memory array [3]. RAM has three ingredient components: an array of memory cells, an address register and an output register. Each cell is addressed with a unique address from 2^n addresses. When the address register is loaded with an address, the corresponding cell content is retrieved via the output register.

RAM is the primary memory in classical computers. Quantum primary memory, QRAM, is the main infrastructure to build a powerful quantum computer. Quantum computer

applications and quantum control systems require creating variables in QRAM. Each variable name is translated to a reserved address that points to a unique location, containing the variable value, in the QRAM. In this paper, we propose a novel QRAM model for storing classical data and quantum data in 2^n different states inside QRAM. The quest of implementing QRAM is essential for the implementation of quantum algorithms [3]–[9]. Moreover, QRAM would provide an exponential speed up for pattern recognition algorithms [11]–[17]. In [18], Giovanetti et al. proposed addressing a QRAM architecture called the "bucket brigade" [18] that needs $O(n)$ to call a memory cell. The nodes of the routing binary tree are represented by three level quantum systems (qutrits) [18]. To study the efficiency of the bucket brigade scheme, Srinivasan et al. [19] showed the circuit model for the quantum bucket brigade architecture and investigated the quantum error correction for the circuit. This QRAM [18] needs a qutrit-based system to be implemented, i.e. it cannot be implemented on qubit-based quantum computers. Recently, D. K. Park et al. [20] proposed Flip-Flop Quantum Random Access Memory (FF-QRAM) based on the quantum circuit model. A main component of a FF-QRAM circuit is the controlled qubit rotation $C^n R_y(\theta^l)$ that must be used to

store data item l [20]. This means that the structure of this QRAM [20] is data dependent. In this paper, we propose a novel efficient quantum random access memory for quantum computers. Unlike FF-QRAM [20], the proposed QRAM has a fixed structure. Also, unlike bucket brigade QRAM [18], the proposed QRAM can be implemented on qubit-based quantum computers. Moreover, the proposed QRAM can be used to efficiently write both known and unknown classical/quantum data. The storage capacity of the proposed QRAM is high compared to that of classical RAM. Furthermore, the proposed model can access arbitrary location in $O(1)$ compared with other state-of-the-art models.

The remainder of this paper is organized as follows. In section 2, we present the proposed QRAM model and the proposed reading and writing algorithm. In section 3, we analyze performance of the new QRAM. Section 4 illustrates the experimental results of the simulation of the proposed QRAM. Finally, section 5 concludes the paper by accentuating its main findings.

II. THE PROPOSED QUANTUM RANDOM ACCESS MEMORY (QRAM) CIRCUIT

A. THE PROPOSED QRAM CIRCUIT

Fig.1 shows the circuit of the proposed Quantum Random Access Memory (QRAM). The register $|A\rangle$ represents the address register used to address the locations of the register $|D\rangle$, so the register $|A\rangle$ determines the locations of the variables in QRAM. The size of the register $|A\rangle$ is n qubits to address $2n$ locations in the QRAM. Consequently, the size of $|D\rangle$ is n qubits, which is used to represent $2n$ locations in the QRAM. Moreover, an extra qubit $|dq\rangle$ is initialized at state $|0\rangle$. $|qy\rangle$ is a $n + m$ qubit-sized bus register, which links the quantum processor/micro-controller and QRAM. The first n qubits of the bus register $|qy\rangle$ are used to carry the address of the variable location provided by a quantum computer or a quantum microcontroller while the other m qubits are used to carry the value in the variable to transfer it to a specific location in the quantum RAM or are used to read the data from QRAM. Finally, an extra qubit $|r\rangle$ is used to distinguish between reading and writing processes. In this model, the correlation between the memory cell and its address occurs via entanglement when the writing process is performed. This QRAM model has the potential to store classical data or a superposition of states into a single location. Hence, the capacity of the proposed model increases exponentially compared to that of classical RAM.

B. THE NEW QRAM READING AND WRITING ALGORITHM

In this section, we present the algorithm that handles reading and writing operations for the proposed QRAM model.

- 1) Register Preparation: $|\psi_0\rangle = H^{\otimes n}|A\rangle^{\otimes n} \otimes I^{\otimes n}|D\rangle^{\otimes n} \otimes I|dq\rangle \otimes I^{\otimes 2n}|qy\rangle^{2n} \otimes I|r\rangle$, such that each register is initialized by the vacuum state $|000\dots 0\rangle$.

- 2) $|\psi_1\rangle = \prod_{i=1}^n NOT_{A_i} C_{qy_i A_i}^{not} |\psi_0\rangle$.
- 3) $|\psi_2\rangle = T_{A_1 A_2 \dots A_n dq}^n |\psi_1\rangle$.
- 4) $|\psi_3\rangle = \prod_{i=1}^n T_{r dq qy_{n+i} D_i}^3 C^0 CSWAP_{r dq y_{n+i} D_i} |\psi_2\rangle$.
- 5) $|\psi_4\rangle = T_{A_1 A_2 \dots A_n dq}^n |\psi_3\rangle$.
- 6) $|\psi_5\rangle = \prod_{i=1}^n NOT_{A_i} C_{qy_i A_i}^{not} |\psi_4\rangle$.

III. PERFORMANCE ANALYSIS OF THE NEW QRAM

- 1) Step1: The algorithm applies n Hadamard gates. Each of them is applied to a single qubit of the register $|A\rangle$ to create a complete superposition of states in the register $|A\rangle$ to address 2^n locations in the QRAM.
- 2) Step 2: When an address is loaded in the first n qubits of the bus register $|qy\rangle$, the QRAM needs to find the address location among 2^n addresses of the register $|A\rangle$, which is assigned by a quantum processor via the bus register $|qy\rangle$. To find this location, a set of n $CNOT$ gates are applied between each qubit of the bus register $|qy\rangle$ as a control qubit and the corresponding qubit in the register $|A\rangle$ as a target qubit. Then, a set of n quantum-NOT gates are applied to the qubits of the register $|A\rangle$ individually. The result of this operation transforms the required location in the register $|A\rangle$ to be in the state $|11\dots 1\rangle$ in the superposition.
- 3) Step 3: The Toffoli gate is used to mark the address that matches the input address in the bus register $|qy\rangle$ by entangling $|dq\rangle$ with the QRAM. The Toffoli gate is defined as

$$T_{A_1 A_2 \dots A_2 dq}^n = |A_1 A_2 \dots A_2 dq, (A_1 A_2 \dots A_2 + dq) \bmod 2\rangle.$$

- 4) Step 4: The QRAM performs a reading or writing process from a given location provided by the quantum processor through the first n^{th} qubits of register $|qy\rangle$ based on the state of the qubit $|r\rangle$ as follows:
 - (i) If the qubit $|r\rangle$ is loaded with state $|1\rangle$ by the quantum processor, then the $CCNOT$ gate is run to copy the value of the variable to the last n^{th} of register $|qy\rangle$. Furthermore, the controlled-controlled-swap gate is not working, so the reading process is complete.
 - (ii) However, if the quantum processor loads the state $|0\rangle$ to the qubit $|r\rangle$, then the controlled-controlled-swap, $C^0 CSWAP_{r dq y_{n+i} D_i}$, gate is applied to write the value stored in the last n qubits of the register $|qy\rangle$ into the QRAM location specified by the first n^{th} qubits. Furthermore, the $CCNOT$ gate is not working, so the writing process is complete. $C^0 CSWAP_{r dq y_{n+i} D_i}$ is the swap gate controlled by qubit $|r\rangle$ and qubit $|dq\rangle$.
- 5) Step 5: Remove the entanglement between qubit $|dq\rangle$ and register $|A\rangle$ by applying the Toffoli gate to disentangle it.
- 6) Step 6: Remove the effect of the first step by applying a set of n $CNOT$ gates between each qubit of the bus

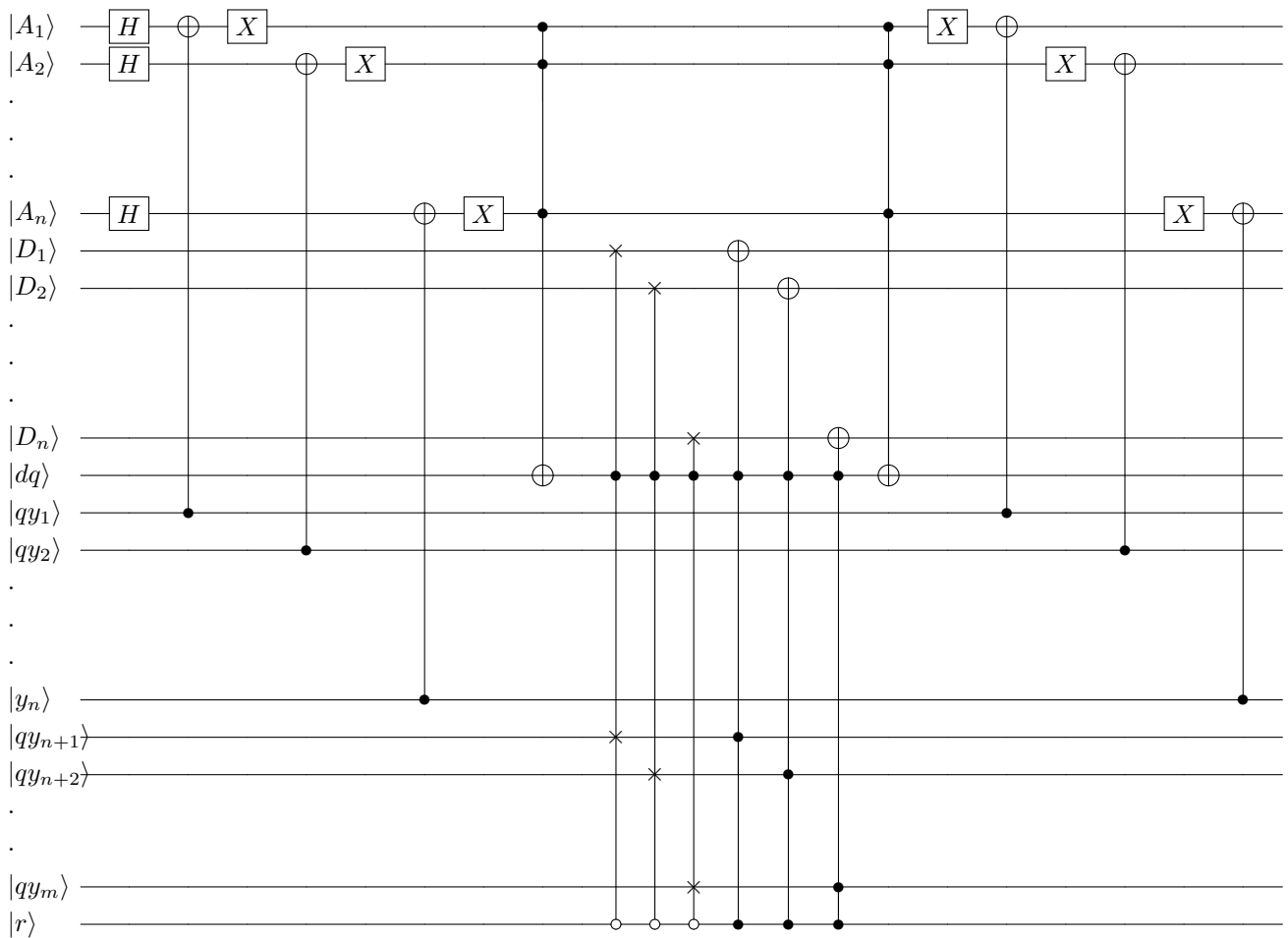


FIGURE 1. A quantum circuit for the proposed quantum random access memory (QRAM).

register $|qy\rangle$ as a control qubit and the corresponding qubit in the register $|A\rangle$ as a target qubit. Then, a set of n quantum-NOT gates are applied on the qubits of register $|A\rangle$ individually.

IV. EXPERIMENTAL REALIZATION OF THE PROPOSED QRAM

To verify the QRAM practically, we will conduct some experiments for writing and reading classical values in the proposed QRAM using the Javantum simulator. First, to simulate the writing process of the proposed QRAM, let us assume that there is an application that performs some tasks using four variables $x, y, u,$ and z . Also, let us assume that this application requires assigning the value 7 (111 in binary) to variable x (that has the address 00). As the number of variables is four, then 2 qubits are needed to address register $|A\rangle$. The simulation results of writing the binary value 111 in the address label 00 are shown in Fig. 2. In this bar chart, the green bars represent the theoretical results, and the red bars represent the Javantum simulator results. Fig. 2 shows that the simulation results are consistent with the theoretical results. Second, to simulate the reading process of the pro-

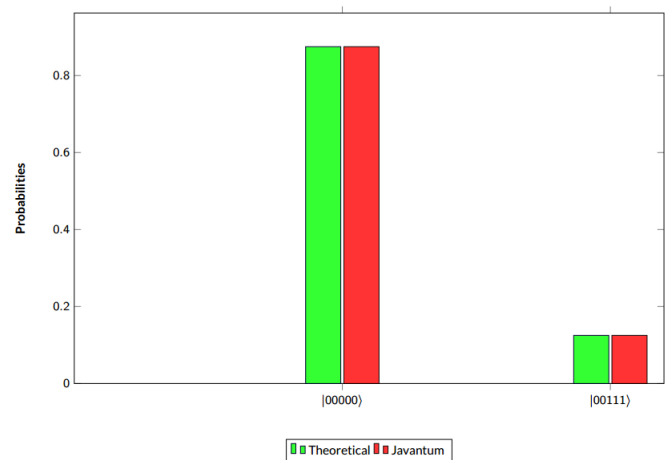


FIGURE 2. Simulation results of writing the classical value 111 in address label 00.

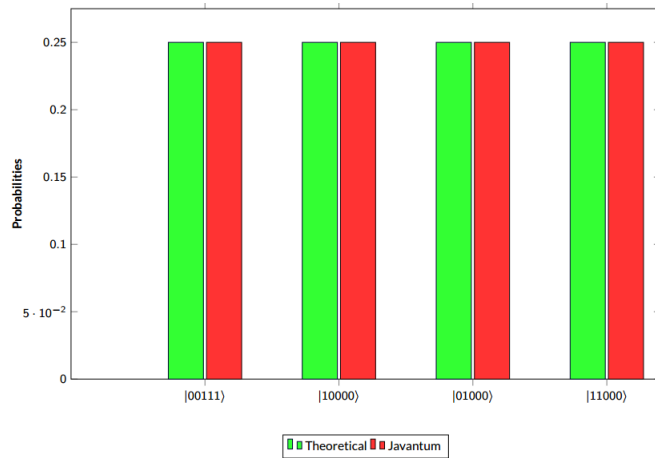


FIGURE 3. Simulation results of reading the value 111 from address label 00.

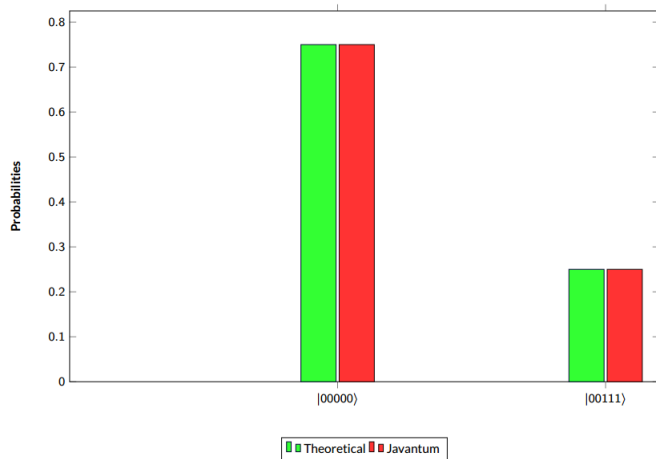


FIGURE 4. Simulation results of writing the quantum state $\sqrt{\frac{1}{2}}|00\rangle + \sqrt{\frac{1}{2}}|11\rangle$ in address label 00.

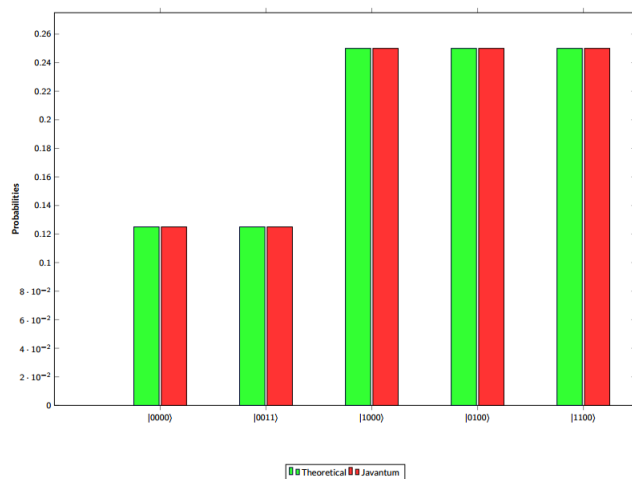


FIGURE 5. Simulation results of reading the quantum state $\sqrt{\frac{1}{2}}|00\rangle + \sqrt{\frac{1}{2}}|11\rangle$ from address label 00.

posed QRAM, we need to read the value of variable x (that has the address “00”) that was written as 111. The simulation results of reading the binary value 111 from address label “00” are shown in Fig. 3. Fig. 3 shows that the simulation results match the theoretical results. Next, we will conduct some experiments for writing and reading quantum states in the proposed QRAM using the Javantum simulator. Third, suppose that it is essential to save state $\sqrt{\frac{1}{2}}|00\rangle + \sqrt{\frac{1}{2}}|11\rangle$ in address label “00”. The simulation results of writing state $\sqrt{\frac{1}{2}}|00\rangle + \sqrt{\frac{1}{2}}|11\rangle$ in address label “00” are shown in Fig. 4. In this bar chart, the green histograms represent the theoretical results, and the red histograms represent the Javantum simulator results. Fig. 4 illustrates that the simulation results match the theoretical results. In the final experiment, it is necessary to read the superposition state, $\sqrt{\frac{1}{2}}|00\rangle + \sqrt{\frac{1}{2}}|11\rangle$, from address label “00”. The simulation results of reading the superposition from address label “00” are given in Fig. 5. The figure shows that the simulations results match the theoretical results. Additionally, the statistical fidelity of the simulation results via the Javantum simulator, which is 0.999971, verify the consistency with the theoretical results (since the optimal fidelity is $F = 1$). Consequently, the results of the four mentioned experiments demonstrate that the proposed QRAM is efficient as a primary memory for quantum computers and can be implemented via different quantum computer platforms. The abovementioned experiments indicate that the proposed QRAM is more efficient than FF-QRAM [20] because it has a fixed structure; uses well-known quantum gates, namely, NOT, CNOT, CCNOT, Toffoli and controlled-controlled-swap gates; and is data independent. In addition, the proposed QRAM does not need qutrit, so it is more efficient to implement via different quantum computer platforms compared with bucket brigade QRAM [18]. Moreover, the complexity of the proposed QRAM calls is $O(1)$ compared with bucket brigade QRAM [18] and FF-QRAM [20], which have $O(n)$ calls and $O(Mn)$ calls, respectively. Hence, the proposed QRAM is faster than other state-of-the-art models. As a result, the superiority of the proposed QRAM is remarkable compared to the existing QRAMs [18], [20].

V. CONCLUSION

In this paper, we proposed a novel QRAM circuit with a fixed structure that can be used to handle reading and writing processes and access arbitrary locations among 2^n locations in $O(1)$. Additionally, it can write data independently and can be used to store both known/unknown classical/quantum data. Moreover, it is proposed based on well-known quantum gates, such as NOT, CNOT, CCNOT, Toffoli, and controlled-controlled-swap gates. In addition, it can be applied to a variety of quantum qubit-based platforms. Finally, the new QRAM is simulated in a quantum computer simulator with a statistical fidelity of 0.999971.

REFERENCES

- [1] J. G. Ren, P. Xu, P., H. L. Yong, et al., Ground-to-satellite quantum teleportation. *Nature* 549, 70–73, 2017
- [2] Bennett, C. H. et al., Teleporting an unknown quantum state via dual classical and Einstein-Podolsky-Rosen channels, *Phys. Rev. Lett.* 70, 1895-1899, 1993
- [3] A. Robert, P.K. Barkoutsos, S. Woerner, et al., Resource-efficient quantum algorithm for protein folding, *npj Quantum Inf* 7, 38, 2021
- [4] L. Huang, H. Zhou, K. Feng, et al., Quantum random number cloud platform, *npj Quantum Inf* 7, 107, 2021
- [5] M. Zidan, A.-H. Abdel-Aty, D. M. Nguyen, A. S. A. Mohamed, Y. Al-Sbou, H. Eleuch, M. Abdel-Aty, Quantum classification algorithm based on competitive learning neural network and entanglement measure, *Results in Physics*, 15, 102549, 2019
- [6] W Liu, Q Wu, J Shen, J Zhao, M Zidan, L Tong, An optimized quantum minimum searching algorithm with sure-success probability and its experiment simulation with Cirq, *Journal of Ambient Intelligence and Humanized Computing*, 1-10, 2021
- [7] A. Robert, P.K. Barkoutsos, S. Woerner et al., Resource-efficient quantum algorithm for protein folding, *npj Quantum Inf*, 7, 38, 2021
- [8] A. Montanaro, Quantum algorithms: an overview, *npj Quantum Inf* 2, 15023, (2016)
- [9] P. W. Shor, Polynomial-time algorithms for prime factorization and discrete logarithms on a quantum computer, In: *Proceedings of the 35th Annual Symposium on Foundations of Computer Science*, Santa Fe, NM, Nov 20–22, 1994
- [10] Mohammed Zidan, H. Eleuch, M. Abdel-Aty, Non-classical computing problems: Toward novel type of quantum computing problems, *Results in Physics*, 21, 103536, 2021
- [11] H. Y. Huang, M. Broughton, M. Mohseni, et al, Power of data in quantum machine learning, *Nat Commun* 12, 2631 (2021).
- [12] D. L. Deng, Machine learning detection of bell nonlocality in quantum many-body systems, *Phys. Rev. Lett.* 120, 240402 (2018).
- [13] M. Zidan, A.-H. Abdel-Aty, M. El-shafei, M. Feraig, Y. Al-Sbou, H. Eleuch, M. Abdel-Aty, Quantum classification algorithm based on competitive learning neural network and entanglement measure, *Applied Sciences* 9 (7), 1277, 2019
- [14] K. Beer, D. Bondarenko, T. Farrelly et al., Training deep quantum neural networks, *Nat Commun* 11, 808, 2020
- [15] V. Nguyen, S. B. Orbell, D.T. Lennon et al, Deep reinforcement learning for efficient measurement of quantum devices, *npj Quantum Inf* 7, 100, 2021
- [16] P. Palittapongarnpim, P. Wittek, E. Zahedinejad, S. Vedaie, B. C. Sanders, Learning in quantum control: High-dimensional global optimization for noisy quantum dynamics, *Neurocomputing* 268, 116–126, 2017
- [17] A. Barr, W. Gispén, A. Lamacraft, Quantum ground states from reinforcement learning, *Proc. Mach. Learn Res* 107, 635–653, 2020
- [18] V. Giovannetti, S. Lloyd, and L. Maccone, Quantum random access memory, *Phys. Rev. Lett.* 100, 160501 (2008)
- [19] S. Arunachalam, V. Gheorghiu, T. J. Connor, M. Mosca, P. V. Srinivasan, On the robustness of bucket brigade quantum RAM, *New Journal of physics*, v 17, 2015,
- [20] D. K. Park, F. Petruccione, J.K.K. Rhee, Circuit-Based Quantum Random Access Memory for Classical Data, *Sci Rep* 9, 3949, 2019



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